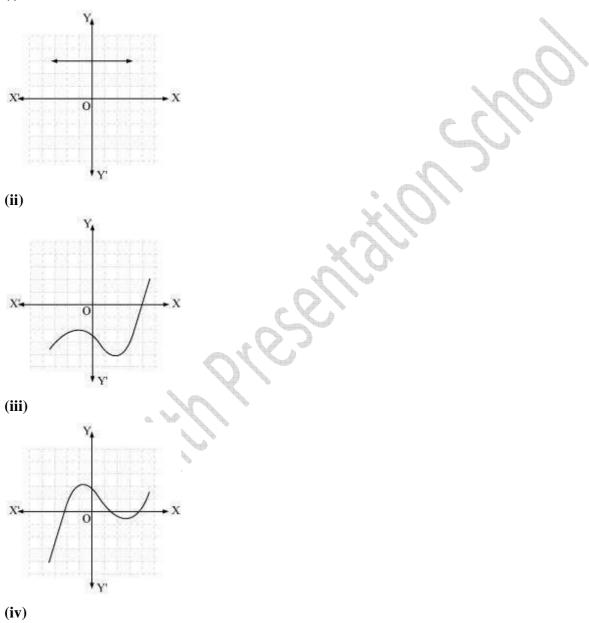
# Polynomials

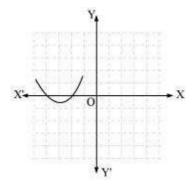
Exercise 2.1 : **Q1**:

The graphs of y = p(x) are given in following figure, for some polynomials p(x). Find the number of zeroes of p(x), in each case.

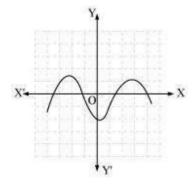
(i)

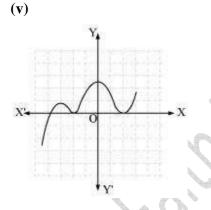


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### Answer :

- (i) The number of zeroes is 0 as the graph does not cut the x-axis at any point.
- (ii) The number of zeroes is 1 as the graph intersects the x-axis at only 1 point.
- (iii) The number of zeroes is 3 as the graph intersects the *x*-axis at 3 points.
- (iv) The number of zeroes is 2 as the graph intersects the *x*-axis at 2 points.
- (v) The number of zeroes is 4 as the graph intersects the *x*-axis at 4 points.
- (vi) The number of zeroes is 3 as the graph intersects the *x*-axis at 3 points.

Exercise 2.2 : Solutions of Questions on Page Number : 33

Find the zeroes of the following quadratic polynomials and verify the relationship between the zeroes and the coefficients.

(i)
$$x^{2}-2x-8$$
 (ii) $4s^{2}-4s+1$  (iii) $6x^{2}-3-7x$   
(iv) $4u^{2}+8u$  (v) $t^{2}-15$  (vi) $3x^{2}-x-4$ 

### Answer :

Q1 :

(i)  $x^2 - 2x - 8 = (x - 4)(x + 2)$ 

The value of  $x^2 - 2x - 8$  is zero when x - 4 = 0 or x + 2 = 0, i.e., when x = 4 or x = -2

Therefore, the zeroes of  $x^2 - 2x - 8$  are 4 and - 2.

$$= 4-2=2=\frac{-(-2)}{1}=\frac{-(\operatorname{Coefficient} \text{ of } x)}{\operatorname{Coefficient} \text{ of } x^2}$$

Sum of zeroes =

Product of zeroes

$$= 4 \times (-2) = -8 = \frac{(-8)}{1} = \frac{\text{Constant term}}{\text{Coefficient of } x^2}$$

(ii)  $4s^2 - 4s + 1 = (2s - 1)^2$ 

The value of  $4s_2 - 4s + 1$  is zero when 2s - 1 = 0, i.e.,

$$s = \frac{1}{2}$$
 Therefore, the zeroes of  $4s_2 - 4s + 1$  are  $\frac{1}{2}$  and  $\frac{1}{2}$ .  
Sum of zeroes =  $\frac{1}{2} + \frac{1}{2} = 1 = \frac{-(-4)}{4} = \frac{-(\text{Coefficient of } s)}{(\text{Coefficient of } s^2)}$   
Product of zeroes  $= \frac{1}{2} \times \frac{1}{2} = \frac{1}{4} = \frac{\text{Constant term}}{\text{Coefficient of } s^2}$   
(iii)  $6x^2 - 3 - 7x = 6x^2 - 7x - 3 = (3x + 1)(2x - 3)$   
The value of  $6x_2 - 3 - 7x$  is zero when  $3x + 1 = 0$  or  $2x - 3 = 0$ , i.e.,  $x = \frac{-1}{3}$  or  $x = \frac{3}{2}$ 

Therefore, the zeroes of  $6x_2 - 3 - 7x$  are  $\frac{-1}{3}$  and  $\frac{3}{2}$ .

Sum of zeroes = 
$$\frac{-1}{3} + \frac{3}{2} = \frac{7}{6} = \frac{-(-7)}{6} = \frac{-(\text{Coefficient of } x)}{\text{Coefficient of } x^2}$$

Product of zeroes =  $\frac{-1}{3} \times \frac{3}{2} = \frac{-1}{2} = \frac{-3}{6} = \frac{\text{Constant term}}{\text{Coefficient of } x^2}$ 

(iv)  $4u^2 + 8u = 4u^2 + 8u + 0$ = 4u(u+2)

The value of  $4u_2 + 8u$  is zero when 4u = 0 or u + 2 = 0, i.e., u = 0 or u = -2Therefore, the zeroes of  $4u_2 + 8u$  are 0 and - 2.

Sum of zeroes =  $0 + (-2) = -2 = \frac{-(8)}{4} = \frac{-(\text{Coefficient of } u)}{\text{Coefficient of } u^2}$ 

Product of zeroes =  $0 \times (-2) = 0 = \frac{0}{4} = \frac{\text{Constant term}}{\text{Coefficient of } u^2}$ 

(v)  $t^2 - 15$ =  $t^2 - 0.t - 15$ =  $(t - \sqrt{15})(t + \sqrt{15})$ 

The value of  $t_2$  - 15 is zero when  $t - \sqrt{15} = 0$  or  $t + \sqrt{15} = 0$ , i.e., when

#### Q2 :

Find a quadratic polynomial each with the given numbers as the sum and product of its zeroes respectively.

(i)  $\frac{1}{4}$ , -1 (ii)  $\sqrt{2}$ ,  $\frac{1}{3}$  (iii)  $0, \sqrt{5}$ 

(iv) 1,1 (v) 
$$-\frac{1}{4},\frac{1}{4}$$
 (vi) 4,1

Answer :

(i)  $\frac{1}{4}, -1$ 

Let the polynomial be  $ax^2 + bx + c$ , and its zeroes be  $\alpha$  and  $\beta$ .

$$\alpha + \beta = \frac{1}{4} = \frac{-b}{a}$$
$$\alpha\beta = -1 = \frac{-4}{4} = \frac{c}{a}$$
If  $a = 4$ , then  $b = -1$ ,  $c = -4$ 

Therefore, the quadratic polynomial is  $4x_2 - x - 4$ .

(ii) 
$$\sqrt{2}, \frac{1}{3}$$

Let the polynomial be  $ax^2 + bx + c$ , and its zeroes be  $\alpha$  and  $\beta$ .

$$\alpha + \beta = \sqrt{2} = \frac{3\sqrt{2}}{3} = \frac{-b}{a}$$
$$\alpha\beta = \frac{1}{3} = \frac{c}{a}$$
If  $a = 3$ , then  $b = -3\sqrt{2}$ ,  $c = 1$ 

Therefore, the quadratic polynomial is  $3x_1 - 3\sqrt{2}x + 1$ .

(iii) 
$$0,\sqrt{5}$$

Let the polynomial be  $ax^2 + bx + c$ , and its zeroes be  $\alpha$  and  $\beta$ .

$$\alpha + \beta = 0 = \frac{0}{1} = \frac{-b}{a}$$
$$\alpha \times \beta = \sqrt{5} = \frac{\sqrt{5}}{1} = \frac{c}{a}$$
If  $a = 1$ , then  $b = 0$ ,  $c = \sqrt{5}$ 

Therefore, the quadratic polynomial is  $x^2 + \sqrt{5}$ .

Let the polynomial be  $ax^2 + bx + c$ , and its zeroes be  $\alpha$  and  $\beta$ .

$$\alpha + \beta = 1 = \frac{1}{1} = \frac{-b}{a}$$
$$\alpha \times \beta = 1 = \frac{1}{1} = \frac{c}{a}$$
If  $a = 1$ , then  $b = -1$ ,  $c$ 

Therefore, the quadratic polynomial is  $x^2 - x + 1$ .

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$$(v) \quad -\frac{1}{4}, \frac{1}{4}$$

Let the polynomial be  $ax^2 + bx + c$ , and its zeroes be  $\alpha$  and

Exercise 2.3 Q1 :

Divide the polynomial p(x) by the polynomial g(x) and find the quotient and remainder in each of the following:

(i) 
$$p(x) = x^3 - 3x^2 + 5x - 3$$
,  $g(x) = x^2 - 2$  (ii)  
 $p(x) = x^4 - 3x^2 + 4x + 5$ ,  $g(x) = x^2 + 1 - x$   
(iii)  $p(x) = x^4 - 5x + 6$ ,  $g(x) = 2 - x^2$ 

Answer :

(i) 
$$p(x) = x^3 - 3x^2 + 5x - 3$$
  
 $q(x) = x^2 - 2$   
 $x^2 - 2) \overline{x^3 - 3x^2 + 5x - 3}$   
 $x^3 - 2x$   
 $- + +$   
 $- 3x^2 + 7x - 3$   
 $- 3x^2 + 6$   
 $+ - -$   
 $7x - 9$ 

Quotient = x - 3Remainder = 7x - 9

(ii) 
$$p(x) = x^4 - 3x^2 + 4x + 5 = x^4 + 0 \cdot x^3 - 3x^2 + 4x + 5$$
  
 $q(x) = x^2 + 1 - x = x^2 - x + 1$ 

Quotient =  $x_2 + x - 3$ 

Remainder = 8

(iii) 
$$p(x) = x^4 - 5x + 6 = x^4 + 0.x^2 - 5x + 6$$
  
 $q(x) = 2 - x^2 = -x^2 + 2$   
 $-x^2 + 2)$ 
 $x^4 + 0.x^2 - 5x + 6$   
 $x^4 - 2x^2$   
 $- +$   
 $2x^2 - 5x + 6$   
 $2x^2 - 4$   
 $- +$   
 $-5x + 10$   
Quotient =  $-x_2 - 2$ 

Quotient =  $-x_2 - 2$ Remainder = -5x + 10

# Q2 :

Verify that the numbers given alongside of the cubic polynomials below are their zeroes. Also verify the relationship between the zeroes and the coefficients in each case:

(i) 
$$2x^3 + x^2 - 5x + 2;$$
  $\frac{1}{2}, 1, -2$   
(ii)  $x^3 - 4x^2 + 5x - 2;$  2, 1, 1

### Answer :

(i)  $p(x) = 2x^3 + x^2 - 5x + 2$ . Zeroes for this polynomial are  $\frac{1}{2}$ , 1, -2  $p(\frac{1}{2}) = 2(\frac{1}{2})^3 + (\frac{1}{2})^2 - 5(\frac{1}{2}) + 2$   $= \frac{1}{4} + \frac{1}{4} - \frac{5}{2} + 2$  = 0  $p(1) = 2 \times 1^3 + 1^2 - 5 \times 1 + 2$  = 0  $p(-2) = 2(-2)^3 + (-2)^2 - 5(-2) + 2$  = -16 + 4 + 10 + 2 = 01

Therefore,  $\overline{2}$ , 1, and - 2 are the zeroes of the given polynomial.

Comparing the given polynomial with  $ax^3 + bx^2 + cx + d$ , we obtain a = 2, b = 1, c = -5, d = 2

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We can take 
$$\alpha = \frac{1}{2}, \beta = 1, \gamma = -2$$
  
 $\alpha + \beta + \gamma = \frac{1}{2} + 1 + (-2) = -\frac{1}{2} = \frac{-b}{a}$   
 $\alpha\beta + \beta\gamma + \alpha\gamma = \frac{1}{2} \times 1 + 1(-2) + \frac{1}{2}(-2) = \frac{-5}{2} = \frac{c}{a}$   
 $\alpha\beta\gamma = \frac{1}{2} \times 1 \times (-2) = \frac{-1}{1} = \frac{-(2)}{2} = \frac{-d}{a}$ 

Therefore, the relationship between the zeroes and the coefficients is verified.

(ii)

Zeroes for this polynomial are 2, 1, 1.

$$p(2) = 2^{3} - 4(2^{2}) + 5(2) - 2$$
  
= 8 - 16 + 10 - 2 = 0  
$$p(1) = 1^{3} - 4(1)^{2} + 5(1) - 2$$
  
= 1 - 4 + 5 - 2 = 0

Therefore, 2, 1, 1 are the zeroes of the given polynomial.

Comparing the given polynomial with  $ax^3 + bx^2 + cx + d$ , we obtain a = 1, b = -4, c = 5, d = -2. Verification of the relationship between zeroes and coefficient of the given polynomial

Sum of zeroes = 2+1+1=4 = 
$$\frac{-(-4)}{1} = \frac{-b}{a}$$

Multiplication of zeroes taking two at a time = (2)(1) + (1)(1) + (2)(1) = 2 + 1 + 2 = 5

$$x_{1-2} = \frac{-(-2)}{1} = \frac{-d}{a}$$

Multiplication of zeroes =  $2 \times 1 \times 1 = 2$  1

Hence, the relationship between the zeroes and the coefficients is verified.

### Q3 :

Check whether the first polynomial is a factor of the second polynomial by dividing the second polynomial by the first polynomial:

(i) 
$$t^2 - 3, 2t^4 + 3t^3 - 2t^2 - 9t - 12$$
  
(ii)  $x^2 + 3x + 1, 3x^4 + 5x^3 - 7x^2 + 2x + 2$   
(iii)  $x^3 - 3x + 1, x^5 - 4x^3 + x^2 + 3x + 1$ 

#### Answer :

(i) 
$$t^2 - 3$$
,  $2t^4 + 3t^3 - 2t^2 - 9t - 12$   
 $t^2 - 3 = t^2 + 0.t - 3$   
 $2t^2 + 3t + 4$   
 $t^2 + 0.t - 3$ )  $2t^4 + 3t^3 - 2t^2 - 9t - 12$   
 $2t^4 + 0.t^3 - 6t^2$   
 $- - +$   
 $3t^3 + 4t^2 - 9t - 12$   
 $3t^3 + 0.t^2 - 9t$   
 $- - +$   
 $4t^2 + 0.t - 12$   
 $4t^2 + 0.t - 12$   
 $- - +$   
 $0$ 

Since the remainder is 0,

Hence, 
$$t^2 - 3$$
 is a factor of  $2t^4 + 3t^3 - 2t^2 - 9t - 12$ .  
(ii)  $x^2 + 3x + 1$ ,  $3x^4 + 5x^3 - 7x^2 + 2x + 2$   
 $x^2 + 3x + 1$ )  $3x^4 + 5x^3 - 7x^2 + 2x + 2$   
 $3x^4 + 9x^3 + 3x^2$   
 $- - -$   
 $-4x^3 - 10x^2 + 2x + 2$   
 $-4x^3 - 12x^2 - 4x$   
 $+ + +$   
 $2x^2 + 6x + 2$   
 $0$ 

Since the remainder is 0,

Hence,  $x^{2} + 3x + 1$  is a factor of  $3x^{4} + 5x^{3} - 7x^{2} + 2x + 2$ (iii)  $x^{3} - 3x + 1$ ,  $x^{5} - 4x^{3} + x^{2} + 3x + 1$  $x^{3} - 3x + 1$ )  $x^{5} - 4x^{3} + x^{2} + 3x + 1$  $x^{5} - 3x^{3} + x^{2}$ 

Since the remainder  $\neq 0$ ,

Hence,  $x^3 - 3x + 1$  is not a factor of  $x^5 - 4x^3 + x^2 + 3x + 1$ .

#### Q4 :

Find a cubic polynomial with the sum, sum of the product of its zeroes taken two at a time, and the product of its zeroes as 2, -7, -14 respectively.

Answer :

Let the polynomial be  $ax^3 + bx^2 + cx + d$  and the zeroes be  $\alpha, \beta$ , and  $\gamma$ . It is given that

$$\alpha + \beta + \gamma = \frac{2}{1} = \frac{-b}{a}$$
$$\alpha\beta + \beta\gamma + \alpha\gamma = \frac{-7}{1} = \frac{c}{a}$$
$$\alpha\beta\gamma = \frac{-14}{1} = \frac{-d}{a}$$

If a = 1, then b = -2, c = -7, d = 14

Hence, the polynomial is  $x^3 - 2x^2 - 7x + 14$ .

Q5 :

Obtain all other zeroes of  $3x^4 + 6x^3 - 2x^2 - 10x - 5$ , if two of its zeroes are  $\sqrt{3}$ 

 $\frac{5}{3}$ 

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and -

# Answer :

$$p(x) = 3x^{4} + 6x^{3} - 2x^{2} - 10x - 5$$
  
Since the two zeroes are  $\sqrt{\frac{5}{3}}$  and  $-\sqrt{\frac{5}{3}}$ ,  
 $\therefore \left(x - \sqrt{\frac{5}{3}}\right) \left(x + \sqrt{\frac{5}{3}}\right) = \left(x^{2} - \frac{5}{3}\right)$   
is a factor of  $3x^{4} + 6x^{3} - 2x^{2} - 10x - 5$ 

Therefore, we divide the given polynomial by 3.

$$x^{2} + 0.x - \frac{5}{3} \underbrace{) \begin{array}{l} 3x^{2} + 6x + 3 \\ 3x^{4} + 6x^{3} - 2x^{2} - 10x - 5 \\ 3x^{4} + 0x^{3} - 5x^{2} \\ - - + \\ 6x^{3} + 3x^{2} - 10x - 5 \\ 6x^{3} + 0x^{2} - 10x \\ - - + \\ 3x^{2} + 0x - 5 \\ 3x^{2} + 0x - 5 \\ - - + \\ - \\ 0 \\ 3x^{4} + 6x^{3} - 2x^{2} - 10x - 5 = \left(x^{2} - \frac{5}{3}\right)(3x^{2} + 6x + 3) \\ = 3\left(x^{2} - \frac{5}{3}\right)(x^{2} + 2x + 1)$$

We factorize  $x^2 + 2x + 1$ 

 $=(x+1)^2$ 

Therefore, its zero is given by x + 1 = 0

x = -1

As it has the term  $(x+1)^2$ , therefore, there will be 2 zeroes at x = -1.

Hence, the zeroes of the given polynomial are  $\sqrt{\frac{5}{3}}$ ,  $-\sqrt{\frac{5}{3}}$ , -1 and -1.

# Q6 :

On dividing  $x^3 - 3x^2 + x + 2$  by a polynomial g(x), the quotient and remainder were x - 2 and -2x + 4, respectively. Find g(x).

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### Answer :

 $p(x) = x^{3} - 3x^{2} + x + 2 \qquad \text{(Dividend)}$ g(x) = ? (Divisor)Quotient = (x - 2)

Remainder = (-2x + 4)Dividend = Divisor × Quotient + Remainder  $x^{3} - 3x^{2} + x + 2 = g(x) \times (x - 2) + (-2x + 4)$   $x^{3} - 3x^{2} + x + 2 + 2x - 4 = g(x)(x - 2)$   $x^{3} - 3x^{2} + 3x - 2 = g(x)(x - 2)$ g(x) is the quotient when we divide  $(x^{3} - 3x^{2} + 3x - 2)$  by (x - 2)

$\begin{array}{c} x^{2} - x + 1 \\ x - 2 \overline{\smash{\big)} x^{3} - 3x^{2} + 3x - 2} \\ x^{3} - 2x^{2} \\ - + \end{array}$	
$\frac{x^{2} - 2x^{2}}{-+$	
$-x^2 + 2x$ $+ -$	
$\begin{array}{c} x-2\\ x-2 \end{array}$	
$\therefore g(x) = (x^2 - x + 1)$	All'

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Q7 :

Give examples of polynomial p(x), g(x), q(x) and r(x), which satisfy the division algorithm and

(i) deg  $p(x) = \deg q(x)$ 

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(ii) deg  $q(x) = \deg r(x)$ 

(iii) deg r(x) = 0

# Answer :

According to the division algorithm, if p(x) and g(x) are two polynomials with  $g(x) \neq 0$ , then we can find polynomials q(x) and r(x) such that  $p(x) = g(x) \times q(x) + r(x)$ , where r(x) = 0 or degree of r(x) < degree of g(x) Degree of a polynomial is the highest power of the variable in the polynomial.

(i) deg p(x) = deg q(x)

Degree of quotient will be equal to degree of dividend when divisor is constant (i.e., when any polynomial is divided by a constant).

Let us assume the division of  $6x^2 + 2x + 2$  by 2.

Here, p(x) =

$$g(x) = 2$$

 $q(x) = 3x^2 + x + 1$  and r(x) = 0

Degree of p(x) and q(x) is the same i.e., 2.

Checking for division algorithm,

$$p(x) = g(x) \times q(x) + r(x)$$

$$6x^2 + 2x + 2 = 2(3x^2 + x + 1)$$

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Thus, the division algorithm is satisfied.

(ii) deg 
$$q(x) = \deg r(x)$$

Let us assume the division of  $x_3 + x$  by  $x_2$ ,

Here,  $p(x) = x_3 + x$ 

 $g(x) = x_2$ 

q(x) = x and r(x) = x

Clearly, the degree of q(x) and r(x) is the same i.e., 1.

Checking for division algorithm,

 $p(x) = g(x) \times q(x) + r(x)$ 

$$x_3 + x = (x_2) \times x + x$$

$$x_3 + x = x_3 + x$$

Thus, the division algorithm is satisfied.

(iii)deg r(x) = 0

Degree of remainder will be 0 when remainder comes to a constant.

Let us assume the division of  $x_3$  + 1by  $x_2$ .

Here, 
$$p(x) = x_{2} + 1$$
  
 $g(x) = x_{2}$   
 $q(x) = x$  and  $r(x) = 1$ 

Clearly, the degree of r(x) is 0.

Checking for division algorithm,

$$p(x) = g(x) \times q(x) + r(x)$$
  

$$x_{3} + 1 = (x_{2}) \times x + 1$$
  

$$x_{3} + 1 = x_{3} + 1$$

Thus, the division algorithm is satisfied.

Exercise 2.4 : Solutions of Questions on Page Number : 37 Q1 :

If the zeroes of polynomial  $x^3 - 3x^2 + x + 1$  are a - b, a, a + b, find a and b.

#### Answer :

$$p(x) = x^3 - 3x^2 + x + 1$$

Zeroes are a - b, a + a + b

Comparing the given polynomial with  $px^3 + qx^2 + rx + t$ , we obtain

p = 1, q = -3, r = 1, t = 1Sum of zeroes = a - b + a + a + b $\frac{-q}{p} = 3a$  $\frac{-(-3)}{1} = 3a$ 3 = 3aa = 1The zeroes are 1 - b, 1, 1 + b. Multiplication of zeroes = 1(1 - b)(1 + b) $\frac{-t}{p} = 1 - b^{2}$  $\frac{-1}{1} = 1 - b^{2}$  $1 - b^{2} = -1$  $1 + 1 = b^{2}$  $b = \pm \sqrt{2}$ 

Hence, a = 1 and  $b = \sqrt{2}$  or  $-\sqrt{2}$ .

### Q2 :

]It two zeroes of the polynomial  $x^4 - 6x^3 - 26x^2 + 138x - 35$  are  $2 \pm \sqrt{3}$ , find other zeroes.

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# Answer :

Given that  $2 + \sqrt{3}$  and  $2 - \sqrt{3}$  are zeroes of the given polynomial. Therefore,  $(x-2-\sqrt{3})(x-2+\sqrt{3}) = x_2 + 4 - 4x - 3$ 

 $= x_2 - 4x + 1$  is a factor of the given polynomial

For finding the remaining zeroes of the given polynomial, we will find the quotient by dividing  $x^4 - 6x^3 - 26x^2 + 138x - 35$  by  $x_2 - 4x + 1$ .

$$\begin{array}{r} x^{2} - 2x - 35 \\ x^{2} - 4x + 1 \overline{\smash{\big)}} x^{4} - 6x^{3} - 26x^{2} + 138x - 35 \\ x^{4} - 4x^{3} + x^{2} \\ - + - \\ - 2x^{3} - 27x^{2} + 138x - 35 \\ - 2x^{3} + 8x^{2} - 2x \\ + - + \\ - 35x^{2} + 140x - 35 \\ - 35x^{2} + 140x - 35 \\ + - + \\ 0 \end{array}$$

Clearly,  $x^4 - 6x^3 - 26x^2 + 138x - 35 = (x^2 - 4x + 1)(x^2 - 2x - 35)$ It can be observed that  $(x^2 - 2x - 35)$  is also a factor of the given polynomial. And  $(x^2 - 2x - 35) = (x - 7)(x + 5)$ 

Therefore, the value of the polynomial is also zero when  $x-7=0_{or} x+5=0$ Or x = 7 or -5

Hence, 7 and - 5 are also zeroes of this polynomial.

Q3 :

If the polynomial  $x^4 - 6x^3 + 16x^2 - 25x + 10$  is divided by another polynomial  $x^2 - 2x + k$ , the remainder comes out to be x + a, find k and a.

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#### Answer :

By division algorithm,

Dividend = Divisor × Quotient + Remainder

Dividend - Remainder = Divisor × Quotient

Dividend - Remainder = Divisor × Quotient  

$$x^4 - 6x^3 + 16x^2 - 25x + 10 - x - a = x^4 - 6x^3 + 16x^2 - 26x + 10 - a$$
 will be perfectly divisible  
by  $x^2 - 2x + k$ .  
Let us divide  $x^4 - 6x^3 + 16x^2 - 26x + 10 - a$  by  $x^2 - 2x + k$ 

Let us divide  $x^4 - 6x^3 + 16x^2 - 26x + 10 - a$  by  $x^2 - 2x + k$ 

$$x^{2}-4x+(8-k)$$

$$x^{2}-2x+k)\overline{x^{4}-6x^{3}+16x^{2}-26x+10-a}$$

$$x^{4}-2x^{3}+kx^{2}$$

$$-\frac{-k--}{-4x^{3}+(16-k)x^{2}-26x}$$

$$-4x^{3}+8x^{2}-4kx$$

$$+\frac{-k}{(8-k)x^{2}-(26-4k)x+10-a}$$

$$(8-k)x^{2}-(16-2k)x+(8k-k^{2})$$

$$-\frac{-k--}{(-10+2k)x+(10-a-8k+k^{2})}$$
It can be observed that
$$(-10+2k)x+(10-a-8k+k^{2})$$
will be 0.
Therefore,
$$(-10+2k)=0$$
 and
$$(10-a-8k+k^{2})=0$$
For
$$(-10+2k)=0$$
And thus,  $k=5$ 
For
$$(10-a-8k+k^{2})=0$$

$$10-a-8k+k^{2})=0$$

$$10-a-8k+k^{2}=0$$

$$10-a-40+25=0$$

- 5 - *a* = 0 Therefore, *a* = - 5 Hence, *k* = 5 and

*a* = - 5